

# Demand Response Shed Variability

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**Sila Kiliccote**, Johanna Mathieu, Duncan Callaway, Livio Fenga, Nathan Addy,  
Deputy, Demand Response Research Center

[skiliccote@lbl.gov](mailto:skiliccote@lbl.gov)

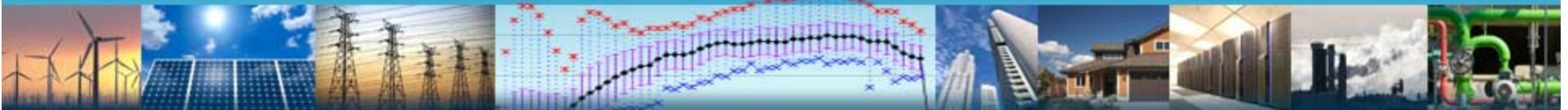
<http://drcc.lbl.gov>



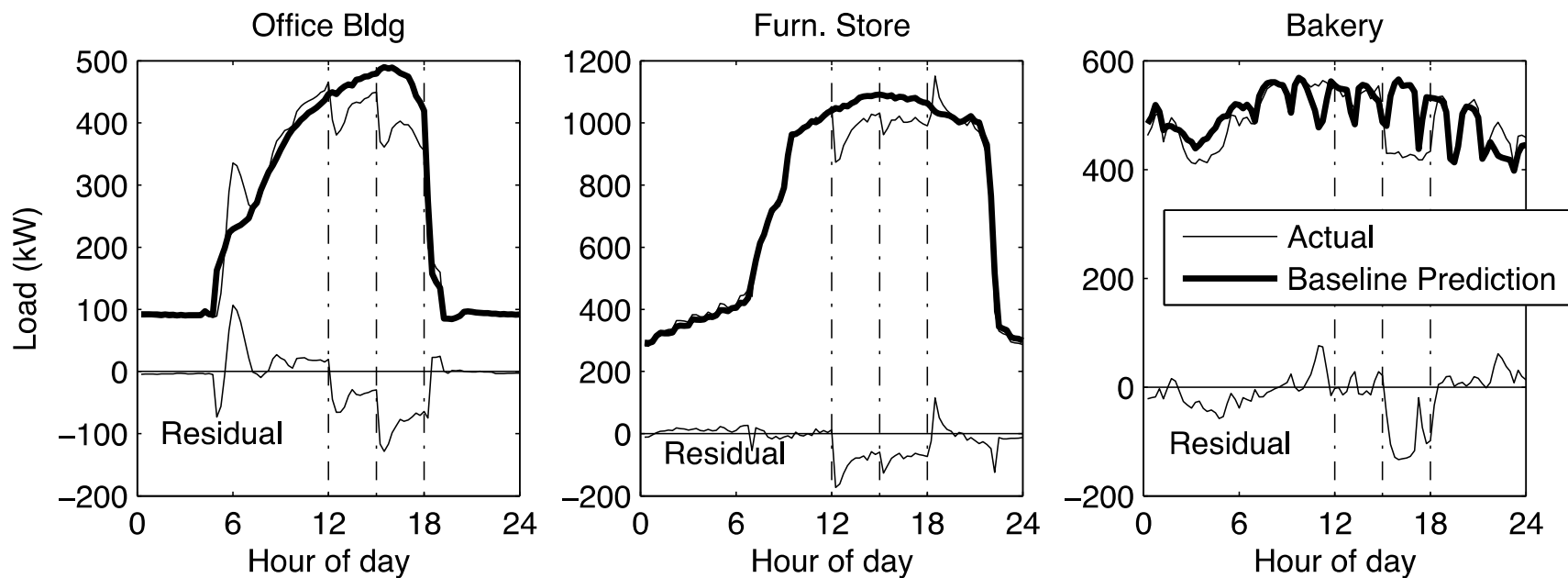
# Outline

- Introduction
  - Research Question
- Methodology
  - Determine Errors on Sheds
  - Define Shed Variability Metric (SVM)
- Results
  - Characterize Facilities with SVM
- Future Work

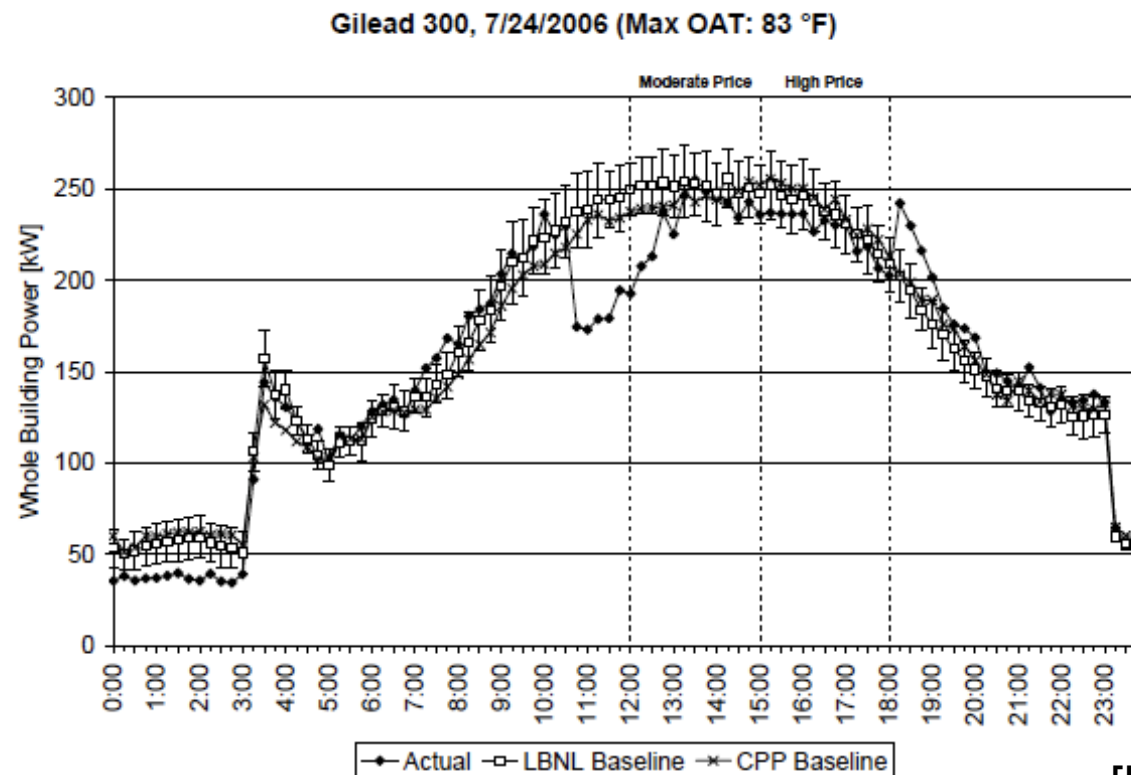
DEMAND RESPONSE RESEARCH CENTER



**DR sheds** are usually estimated by subtracting **actual measured load (kW)** from load predicted by a **baseline model**



Sheds are generally reported **without** uncertainty bounds, even if some sort of error analysis has been done.



[Piette et al. 2007]

Date	Price Level	kW		W/ft <sup>2</sup>		WBP%	
		Max	Ave	Max	Ave	Max	Ave
Jul-24	Moderate Price	49	20	0.59	0.24	19%	8%
	High Price	22	14	0.27	0.16	9%	6%

**Figure ES.4 Average Hourly CPP Load Impacts by Event – PG&E**

[Braithwait et al. 2010]

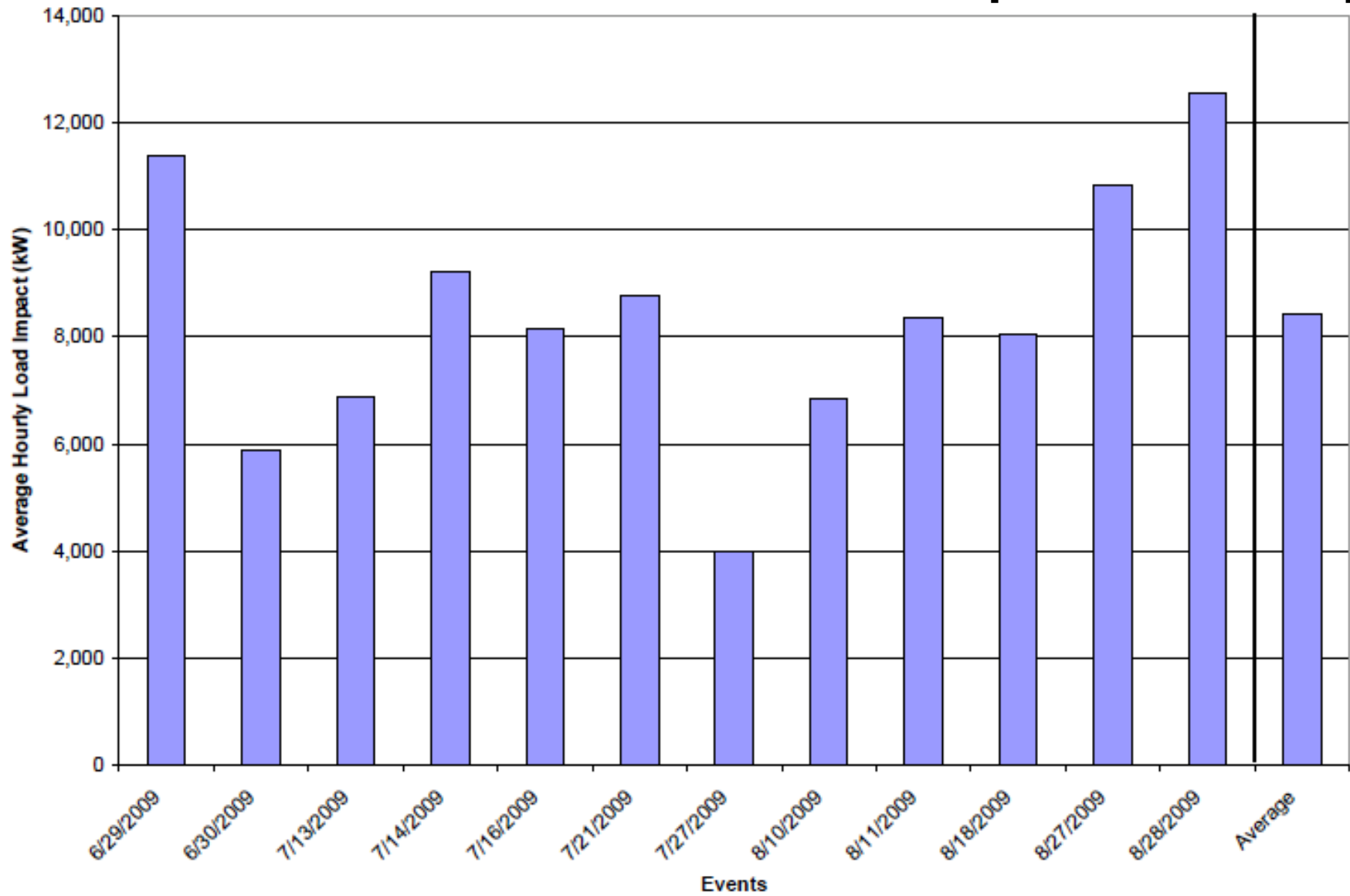


Figure ES.4 Average Hourly CPP Load Impacts by Event – PG&E

[Braithwait et al. 2010]

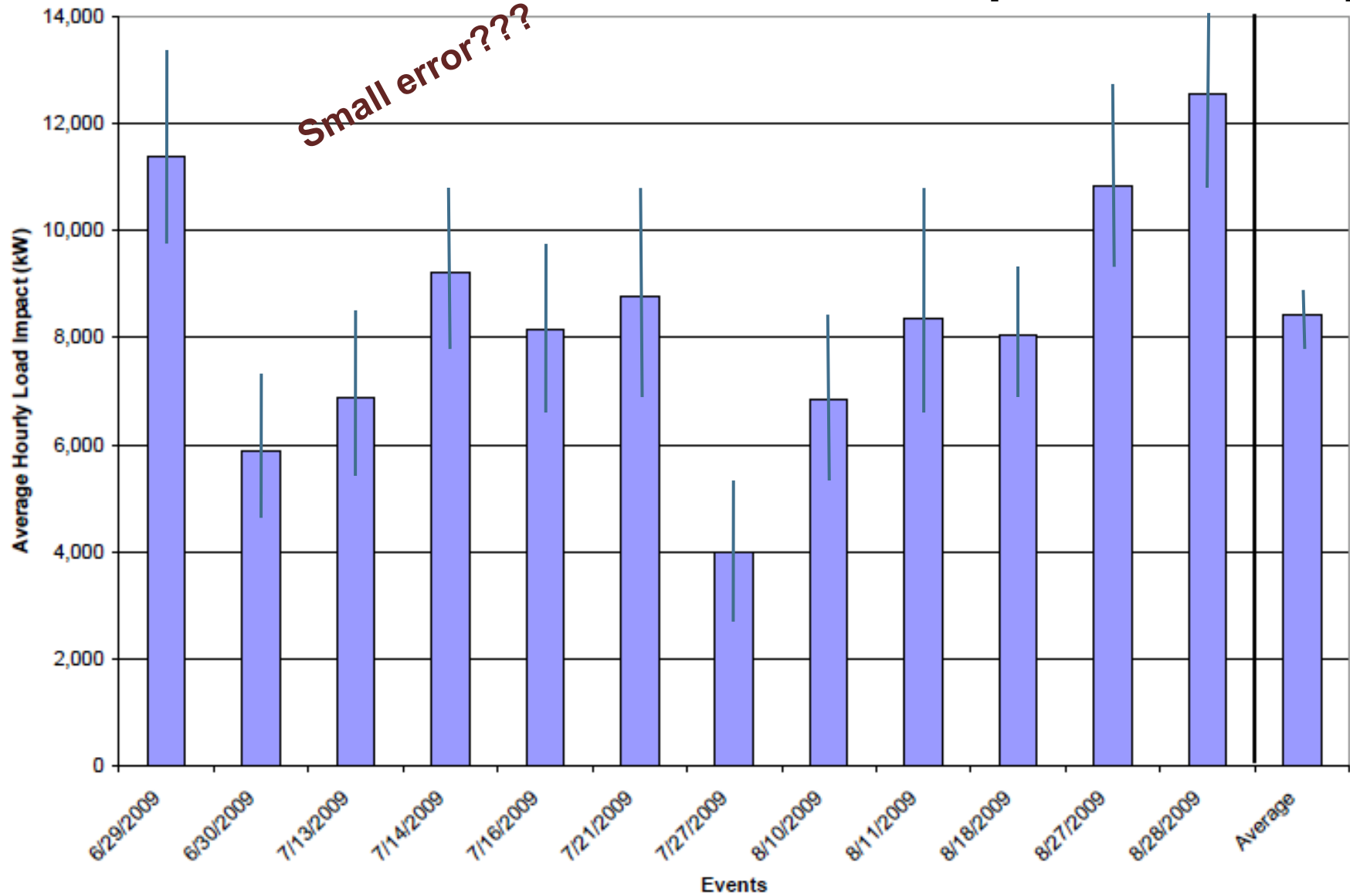
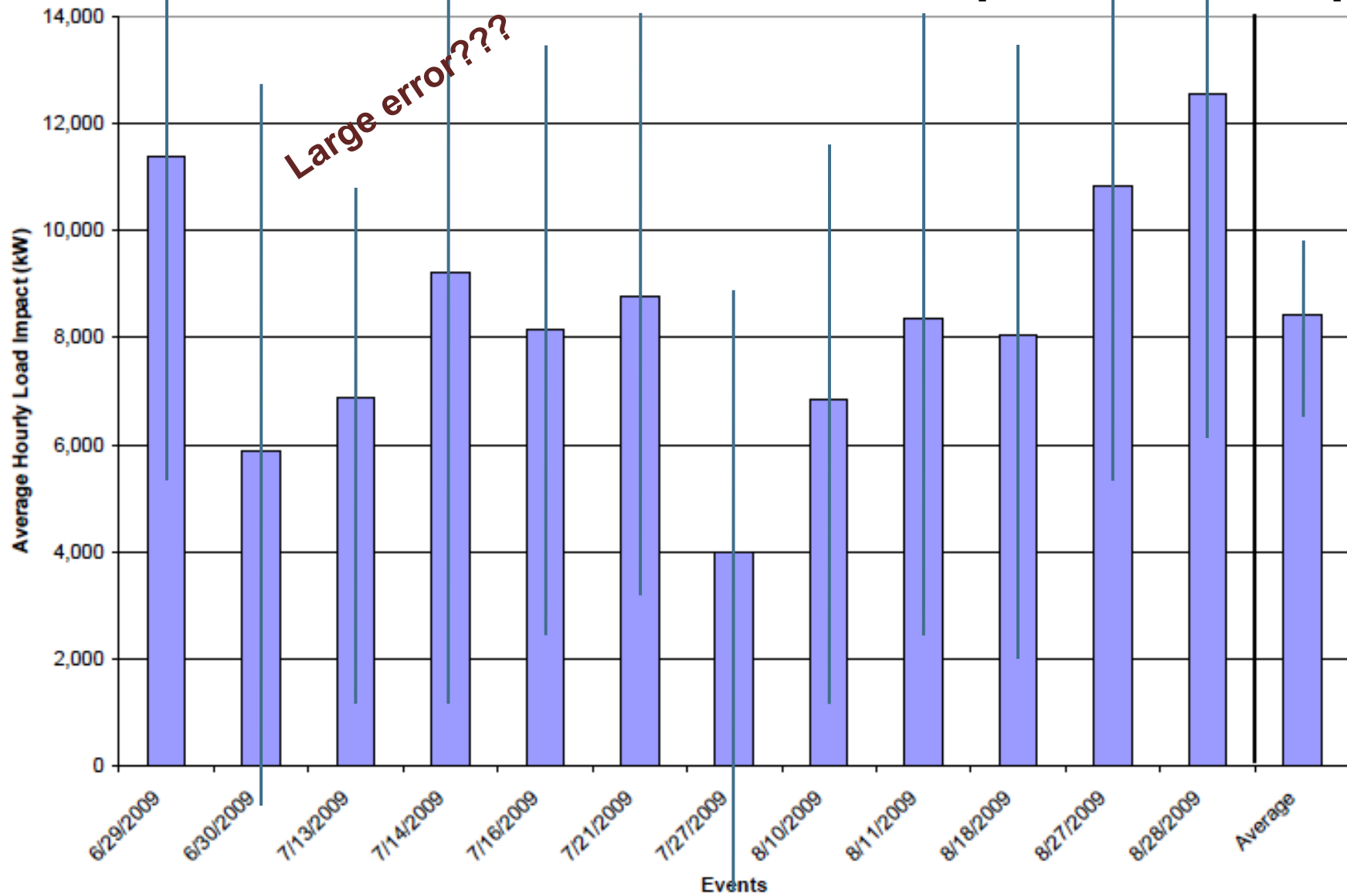


Figure ES.4 Average Hourly CPP Load Impacts by Event – PG&E

[Braithwait et al. 2010]



## Why does understanding 'real' versus 'observed' variability matter?

- **At the aggregate level**

- Real variability could cause frequency/resource adequacy issues
- Observed variability can affect policy
- Variability affects Measurement & Verification
- Participation in DR bidding programs & ancillary services markets

- **At the individual facility level**

- DR performance feedback
- Variability affects Measurement & Verification
- Participation in DR bidding programs and ancillary services markets



## Research Questions:

- How big is baseline model error?
- Is observed shed variability the result of real variability or simply model error?

## Methodology:

- Determine errors on sheds
- Define shed variability metric
- Characterize facilities and aggregate populations by shed variability metric

# Baseline Models

## Common Models

### ○ Averaging

- 3/10, Average of the 3 non-DR days with the highest energy use out of the last 10 non-DR days
- 10/10, Average of the last 10 non-DR days

### ○ Regression, built with non-DR days

- Time-of-day, day-of-week indicator variables
- Linear temperature dependence

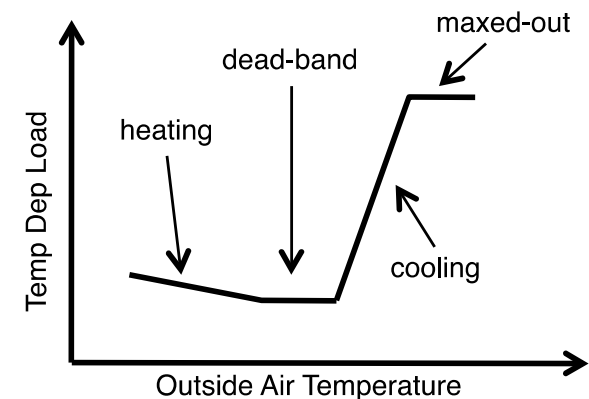
## Our Model

### ○ Regression, built with non-DR days

- Time-of-week indicator variables
- Piecewise linear temperature dependence

$$\text{Occupied: } \hat{L}_o(t_i, T(t_i)) = \alpha_i + \sum_{j=1}^6 \beta_j T_{c,j}(t_i)$$

$$\text{Unoccupied: } \hat{L}_u(t_i, T(t_i)) = \alpha_i + \beta_u T(t_i)$$



[Mathieu et al. 2011,  
*IEEE Trans on Smart  
Grid*]

# DR Parameters

1. Average Demand Shed 1 (kW)

Baseline minus actual average demand 12-3pm

2. Average Demand Shed 2 (kW)

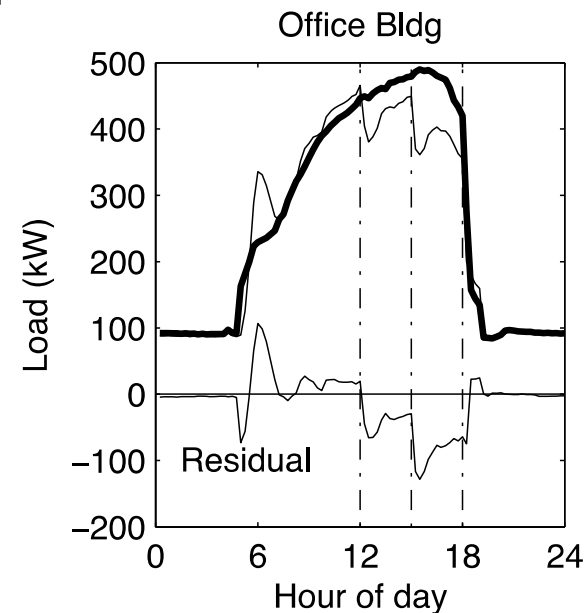
actual average

demand 3-6pm

Baseline minus

Others we identified in the paper:

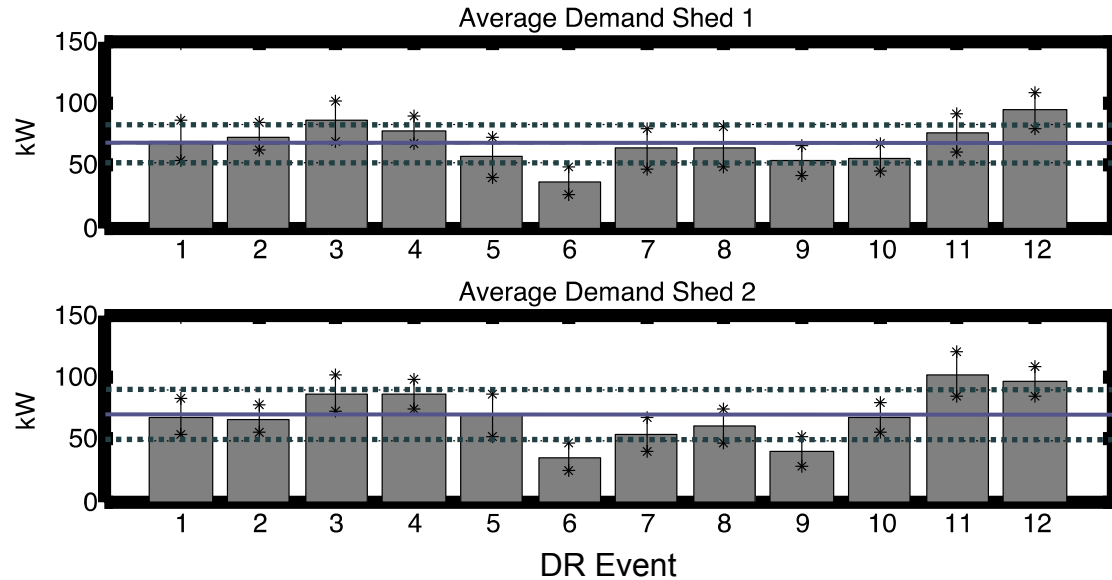
- Daily Peak Demand
- Rebound
- Daily Energy



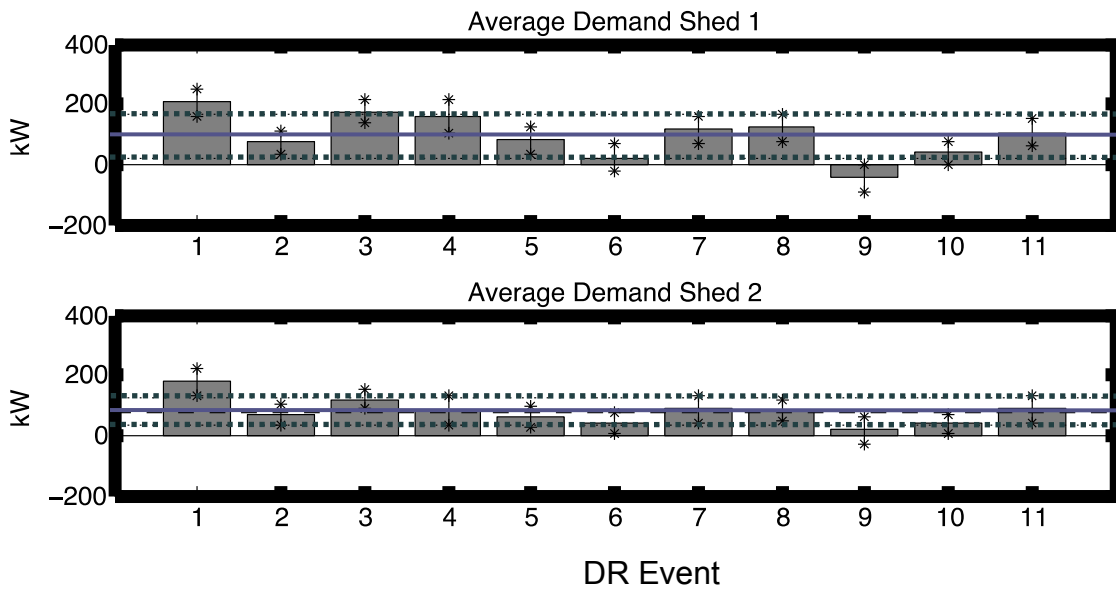
# Errors on DR Sheds

$$Y = \alpha x + \beta + \varepsilon$$




- Standard practice:
  - use the standard error on the regression coefficients,  $\alpha$  and  $\beta$   
(e.g., Fels 1986, Braithwait et al. 2010, Kissock and Eger 2008)  
*BUT... the standard errors underestimate the true error due to autocorrelation and heteroscedasticity of the regression residuals.*
  - Compute the standard deviation of the regression residuals,  $\varepsilon$   
(e.g., Piette et al. 2007)  
*BUT... the regression residuals are self-influenced.*
- We use 'Leave One Out Cross Validation' (LOOCV).



County Bldg 2009



Retail Store 2008

-  Error bars (1 Std Dev)
-  Mean of all events
-  Std Dev (1) of all events

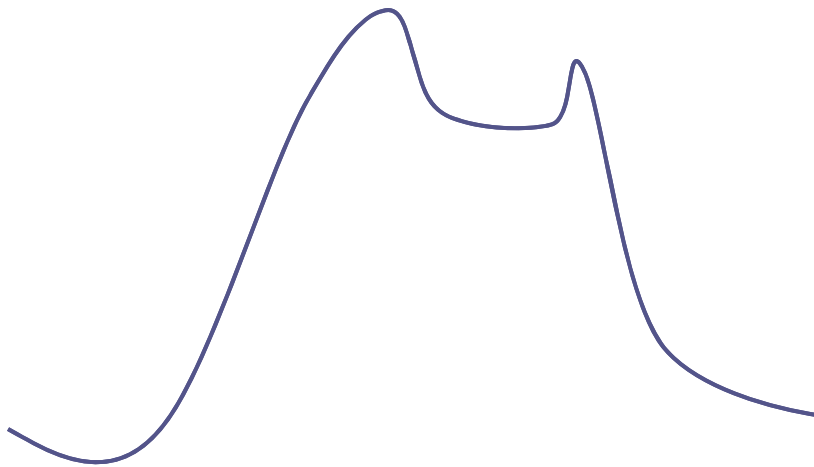
# Shed Variability Metric (SVM) Derivation

What is the variance of the real shed,  $\text{Var}(RS)$ ?

# Shed Variability Metric (SVM) Derivation

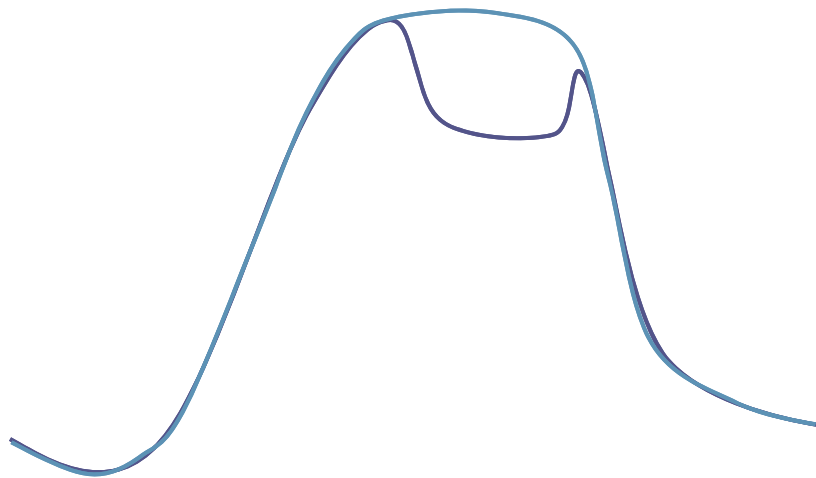
What is the variance of the real shed,  $\text{Var}(RS)$ ?

Observed Load ( $OL$ )



# Shed Variability Metric (SVM) Derivation

What is the variance of the real shed,  $\text{Var}(RS)$ ?

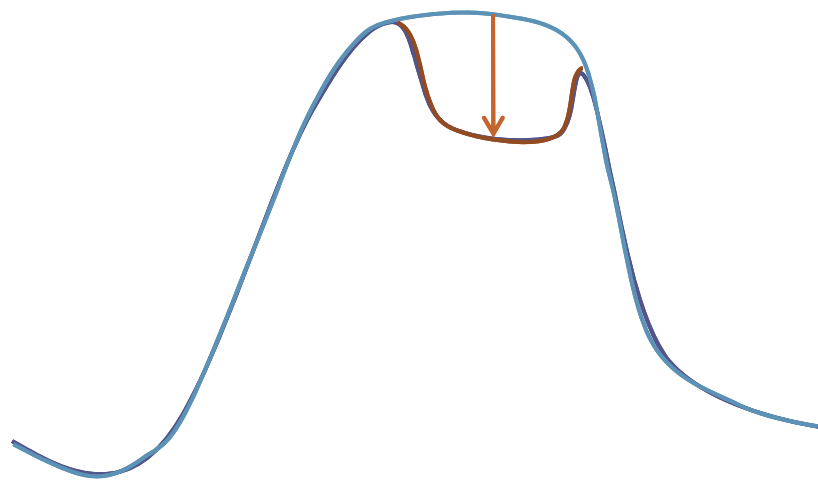


Observed Load (*OL*)  
Real Baseline Load (*RBL*)



# Shed Variability Metric (SVM) Derivation

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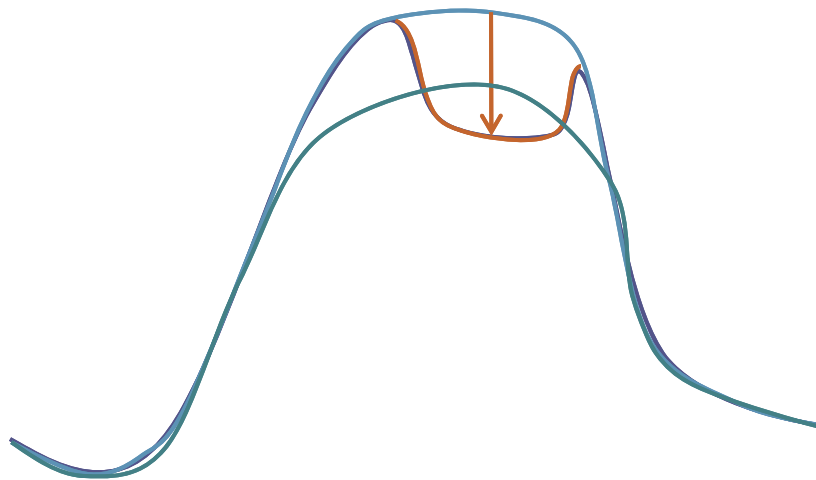


Observed Load ( $OL$ )  
Real Baseline Load ( $RBL$ )  
Real Shed ( $RS$ )

$$OL = RBL - RS$$

# Shed Variability Metric (SVM) Derivation

What is the variance of the real shed,  $\text{Var}(RS)$ ?

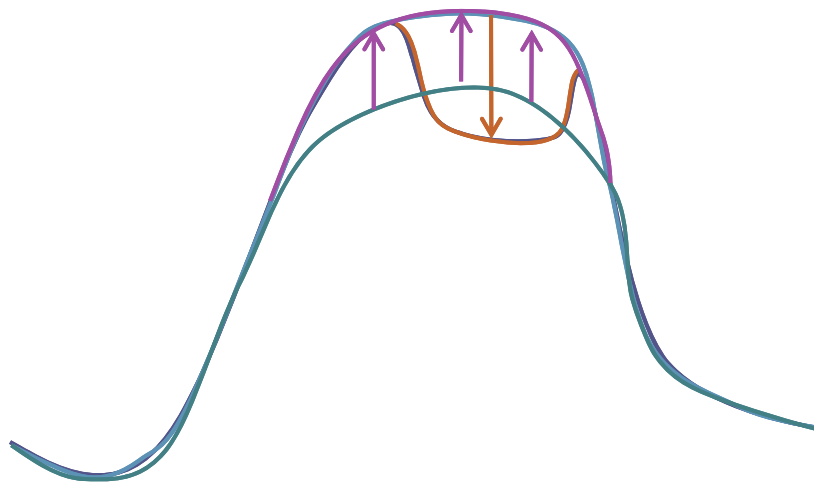


Observed Load ( $OL$ )  
Real Baseline Load ( $RBL$ )  
Real Shed ( $RS$ )  
Predicted Baseline Load ( $PBL$ )

$$OL = RBL - RS$$

# Shed Variability Metric (SVM) Derivation

## What is the variance of the real shed, $\text{Var}(RS)$ ?



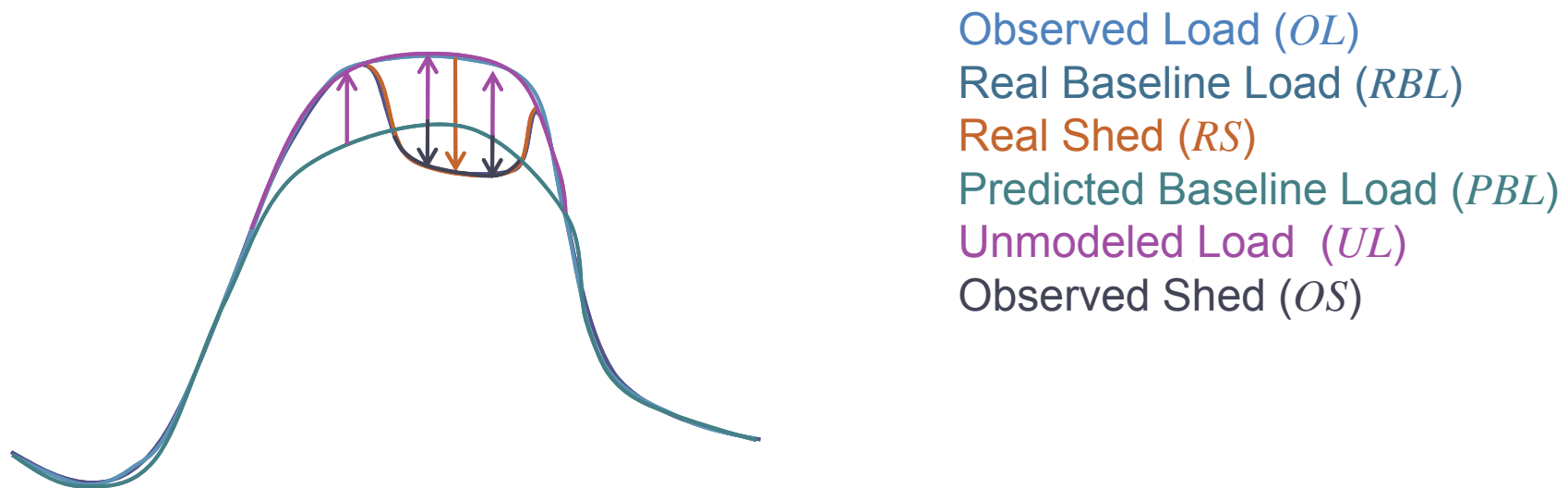
Observed Load (*OL*)  
Real Baseline Load (*RBL*)  
Real Shed (*RS*)  
Predicted Baseline Load (*PBL*)  
Unmodeled Load (*UL*)

$$OL = RBL - RS$$

$$RBL = PBL + UL$$

# Shed Variability Metric (SVM) Derivation

## What is the variance of the real shed, $\text{Var}(RS)$ ?



$$OL = RBL - RS$$

$$RBL = PBL + UL$$

$$OS = OL - PBL$$

- Rearranging and cancelling terms...

$$\text{Observed Shed (OS)} = \text{Unmodeled Load (UL)} - \text{Real Shed (RS)}$$

- Taking the variance of both sides...

$$\text{Var(OS)} = \text{Var(UL)} + \text{Var(RS)} - 2 * \text{Cov(UL, RS)}$$

- Defining the SVM...

$$\text{SVM} := \text{Var(OS)} - \text{Var(UL)} = \text{Var(RS)} - 2 * \text{Cov(UL, RS)}$$

Computabl

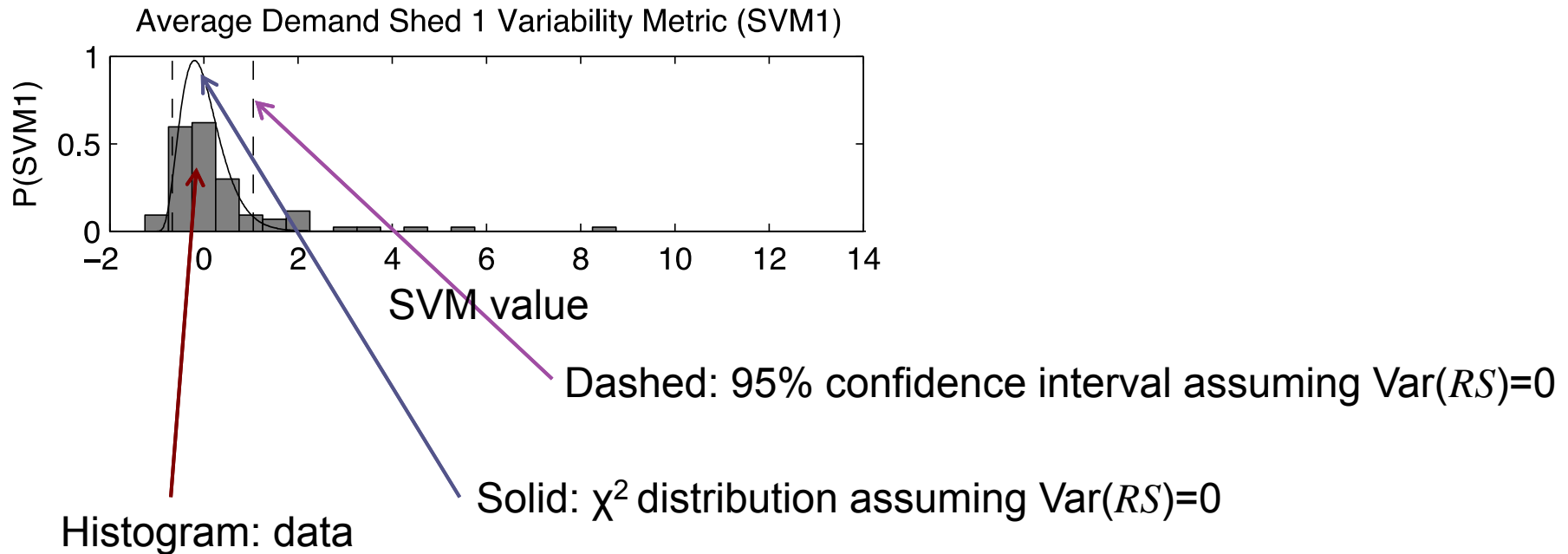
What we're  
after!

Complicating  
term

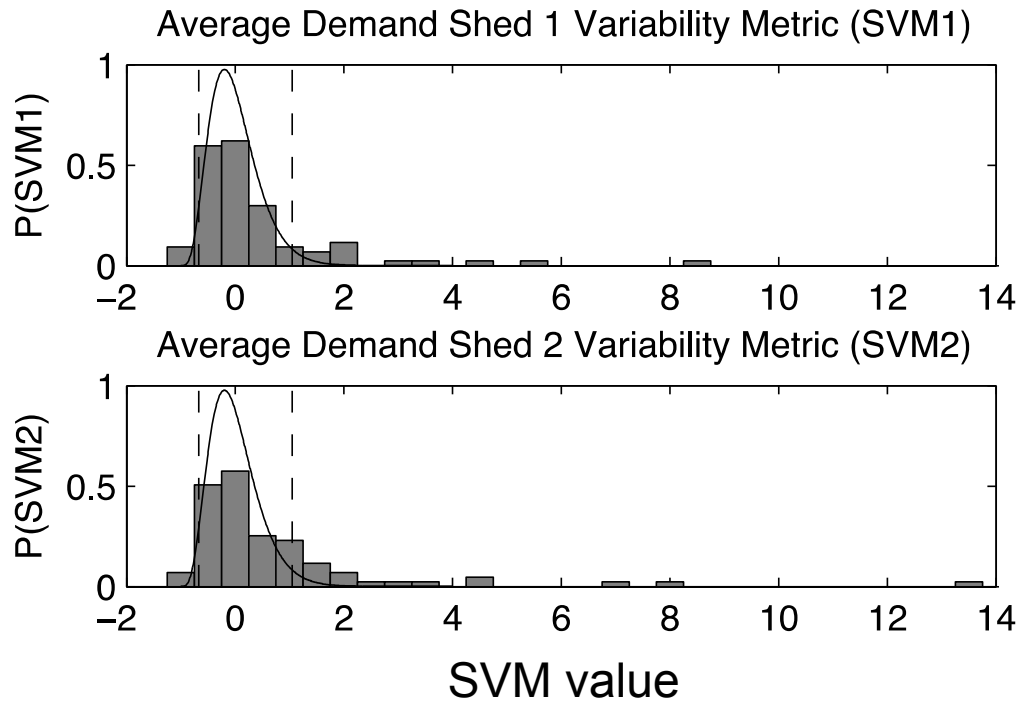
- Finally...

normalize raw power measurements so that  $\text{Var(UL)}=1$

# SVMs for 87 individual facility-years



# SVMs for 87 individual facility-years

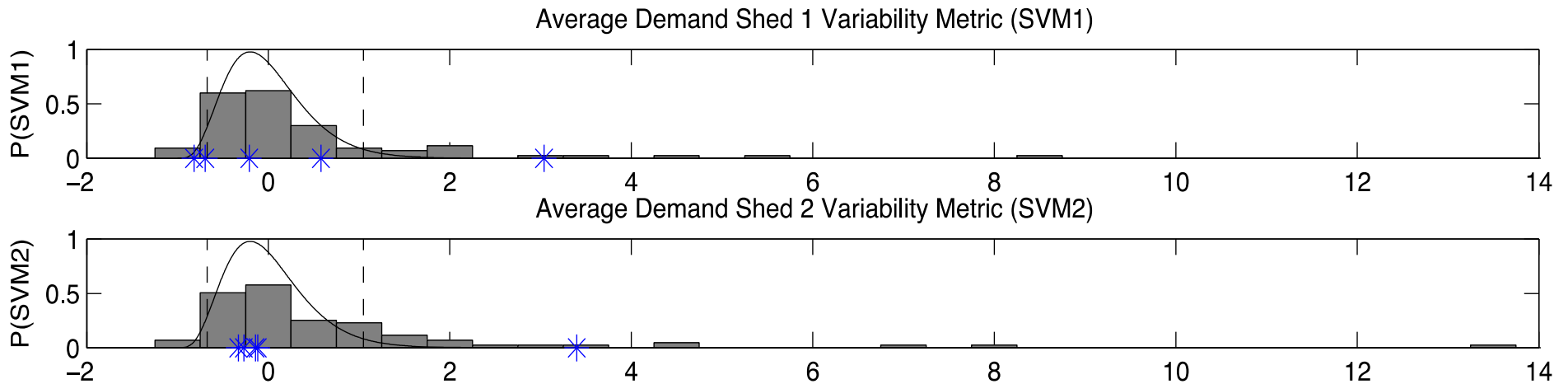


Number (percent) of facility-years with SVMs inside and outside the 95% confidence interval bounds

Metric	Inside Bounds	Outside Bounds
SVM1	65 (75%)	22 (25%)
SVM2	62 (71%)	25 (29%)

# Variability Metrics for the Aggregate Populations

\* aggregate system results



Bold values indicated p-values  $\leq 0.05$

Year	Facilities (Peak <sup>a</sup> )	Shed 1		Shed 2	
		SVM1	p-value	SVM2	p-value
2006 (Zone 1)	4 (2.7 MW)	<b>-0.819</b>	<b>(0.01)</b>	-0.269	(0.67)
2006 (Zone 2)	8 (8.4 MW)	<b>3.039</b>	<b>(&lt;0.01)</b>	<b>3.399</b>	<b>(&lt;0.01)</b>
2007	13 (11.7 MW)	0.579	(0.21)	-0.117	(0.90)
2008	21 (14.6 MW)	-0.210	(0.72)	-0.142	(0.86)
2009	32 (26.9 MW)	<b>-0.696</b>	<b>(0.03)</b>	-0.331	(0.46)



# Findings

- DR parameter results reported without uncertainty estimates can be misleading.
- Observed variability is driven, in large part, by model error.
- Some facilities exhibit real variability.
- In some cases, the aggregate population exhibits real variability, resulting in implications for the system operator with respect to resource planning and system frequency.

## Extended and Future Work

- Implementation of the same methodology to SDG&E and SCE's AutoDR program participants
  - more and diverse data sets
- Better models
  - Reg-SARIMA-X + 4 others

# Thank you!

Sila Kiliccote  
[skiliccote@lbl.gov](mailto:skiliccote@lbl.gov)  
<http://drrc.lbl.gov>